AIEEE-CBSE-ENG-03

1. A function f from the set of natural numbers to integers defined by

$$f(n) = \begin{cases} \frac{n-1}{2}, & \text{when is odd} \\ -\frac{n}{2}, & \text{when n is even} \end{cases}$$

(A) one-one but not onto

- (B) onto but not one-one
- (C) one-one and onto both
- (D) neither one-one nor onto

2. Let z_1 and z_2 be two roots of the equation $z^2 + az + b = 0$, z being complex. Further, assume that the origin, z_1 and z_2 form an equilateral triangle, then

(A) $a^2 = b$

(B) $a^2 = 2b$

(C) $a^2 = 3b$

(D) $a^2 = 4b$

3. If z and ω are two non–zero complex numbers such that $|z\omega|=1$, and Arg (z) – Arg (ω) = $\frac{\pi}{2}$,

then \overline{z}_{ω} is equal to

(A) 1

(B) - 1

(C) i

(D) - i

4. If $\left(\frac{1+i}{1-i}\right)^x = 1$, then

- (A) x = 4n, where n is any positive integer
- (B) x = 2n, where n is any positive integer
- (C) x = 4n + 1, where n is any positive integer
- (D) x = 2n + 1, where n is any positive integer

5. If $\begin{vmatrix} a & a^2 & 1+a^3 \\ b & b^2 & 1+b^3 \\ c & c^2 & 1+c^3 \end{vmatrix} = 0$ and vectors (1, a, a^2) (1, b, b^2) and (1, c, c^2) are non-coplanar, then the

product abc equals

(A) 2

(B) - 1

(C) 1

(D) 0

6. If the system of linear equations

$$x + 2ay + az = 0$$

$$x + 3by + bz = 0$$

$$x + 4cy + cz = 0$$

has a non-zero solution, then a, b, c

(A) are in A. P.

(B) are in G.P.

(C) are in H.P.

(D) satisfy a + 2b + 3c = 0

7. If the sum of the roots of the quadratic equation $ax^2 + bx + c = 0$ is equal to the sum of the squares of their reciprocals, then $\frac{a}{c}$, $\frac{b}{a}$ and $\frac{c}{b}$ are in

(A) arithmetic progression

(B) geometric progression

(C) harmonic progression

(D) arithmetic–geometric–progression

8. The number of real solutions of the equation $x^2 - 3|x| + 2 = 0$ is

(A) 2

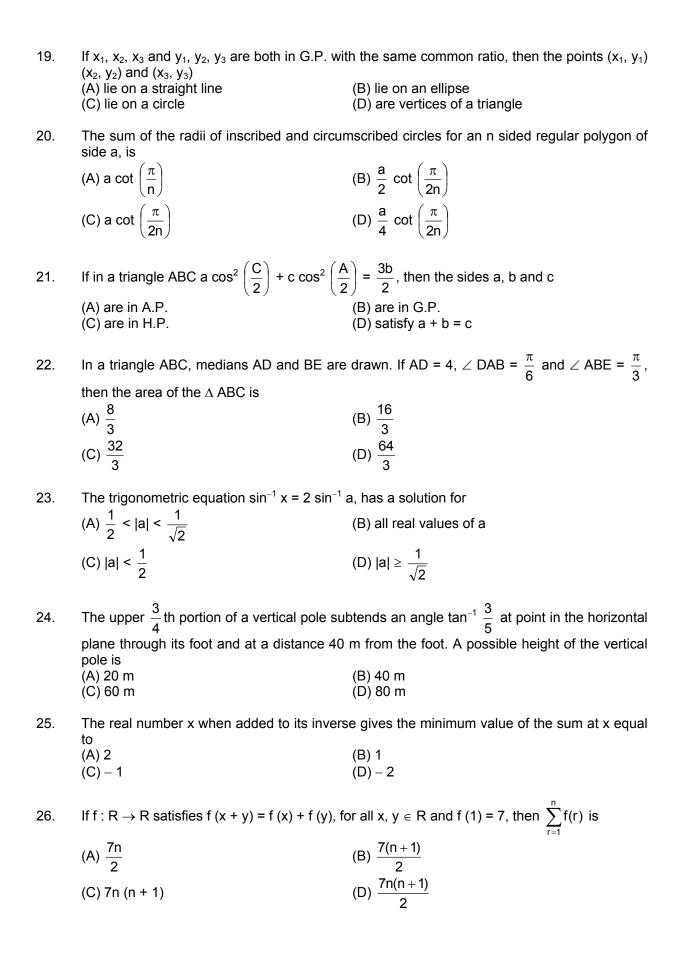
(B) 4

(C) 1

(D) 3

| 9. | The value of 'a' for which one root of the quadratic equation $(a^2 - 5a + 3) x^2 + (3a - 1) x + 2 = 0$ is twice as large as the other, is | | |
|------|---|---|--|
| | | $(B) - \frac{2}{3}$ | |
| | (A) $\frac{2}{3}$ (C) $\frac{1}{3}$ | (D) $-\frac{1}{3}$ | |
| I10. | If $A = \begin{bmatrix} a & b \\ b & a \end{bmatrix}$ and $A^2 = \begin{bmatrix} \alpha & \beta \\ \beta & \alpha \end{bmatrix}$, then | | |
| | (A) $\alpha = a^2 + b^2$, $\beta = ab$ (C) $\alpha = a^2 + b^2$, $\beta = a^2 - b^2$ | (B) $\alpha = a^2 + b^2$, $\beta = 2ab$ (D) $\alpha = 2ab$, $\beta = a^2 + b^2$ | |
| 11. | A student is to answer 10 out of 13 question least 4 from the first five questions. The number (A) 140 (C) 280 | ns in an examination such that he must choose at mber of choices available to him is (B) 196 (D) 346 | |
| 12. | The number of ways in which 6 men and women are to sit together is given by (A) $6! \times 5!$ (C) $5! \times 4!$ | d 5 women can dine at a round table if no two (B) 30 (D) $7! \times 5!$ | |
| 13. | If 1, ω , ω^2 are the cube roots of unity, then $\Delta = \begin{vmatrix} 1 & \omega^n & \omega^{2n} \\ \omega^n & \omega^{2n} & 1 \\ \omega^{2n} & 1 & \omega^n \end{vmatrix}$ is equal to | | |
| | (A) 0 (C) ω | (B) 1 (D) ω ² | |
| 14. | If ${}^{n}C_{r}$ denotes the number of combinations of n things taken r at a time, then the expression ${}^{n}C_{r+1} + {}^{n}C_{r-1} + 2 \times {}^{n}C_{r}$ equals | | |
| | $(A)^{n+2}C_r$ $(C)^{n+1}C_r$ | (B) $^{n+2}C_{r+1}$ (D) $^{n+1}C_{r+1}$ | |
| 15. | The number of integral terms in the expansion of $(\sqrt{3} + \sqrt[8]{5})^{256}$ is (A) 32 (B) 33 | | |
| | (C) 34 | (D) 35 | |
| 16. | If x is positive, the first negative term in the (A) 7 th term (C) 8 th term | expansion of $(1 + x)^{27/5}$ is (B) 5^{th} term (D) 6^{th} term | |
| 17. | The sum of the series $\frac{1}{1\cdot 2} - \frac{1}{2\cdot 3} + \frac{1}{3\cdot 4} - \dots$ upto ∞ is equal to | | |
| | (A) 2 log _e 2 | (B) $\log_2 2 - 1$ | |
| | (C) log _e 2 | (D) $\log_{e}\left(\frac{4}{e}\right)$ | |
| 18. | Let f (x) be a polynomial function of seconthen f' (a), f' (b) and f' (c) are in (A) A.P. (C) H. P. | d degree. If f (1) = f (-1) and a, b, c are in A. P., (B) G.P. (D) arithmetic–geometric progression | |

9.



27. If f (x) = xⁿ, then the value of f (1)
$$-\frac{f'(1)}{1!} + \frac{f''(1)}{2!} - \frac{f'''(1)}{3!} + ... + \frac{(-1)^n f^n(1)}{n!}$$
 is

(A) 2ⁿ
(B) 2ⁿ⁻¹
(C) 0
(D) 1

- 28. Domain of definition of the function $f(x) = \frac{3}{4 x^2} + \log_{10}(x^3 x)$, is

 (A) (1, 2) (B) (-1, 0) \cup (1, 2)
 - (A) (1, 2) (B) $(-1, 0) \cup (1, 2)$ (C) $(1, 2) \cup (2, \infty)$ (D) $(-1, 0) \cup (1, 2) \cup (2, \infty)$
- 29. $\lim_{x \to \pi/2} \frac{\left[1 \tan\left(\frac{x}{2}\right)\right] \left[1 \sin x\right]}{\left[1 + \tan\left(\frac{x}{2}\right)\right] \left[\pi 2x\right]^3}$ is $(A) \frac{1}{8}$ (B) 0
 - (C) $\frac{1}{32}$ (D) ∞
- 30. If $\lim_{x\to 0} \frac{\log(3+x) \log(3-x)}{x} = k$, the value of k is
 - (A) 0 (B) $-\frac{3}{3}$
 - (C) $\frac{2}{3}$ (D) $-\frac{2}{3}$
- 31. Let f(a) = g(a) = k and their n^{th} derivatives $f^n(a)$, $g^n(a)$ exist and are not equal for some n. Further if $\lim_{x\to a} \frac{f(a)g(x)-f(a)-g(a)f(x)+g(a)}{g(x)-f(x)} = 4$, then the value of k is
 - (A) 4 (B) 2 (D) 0
- 32. The function $f(x) = \log (x + \sqrt{x^2 + 1})$, is (A) an even function (B) an odd function (C) a periodic function (D) neither an even nor an odd function
- 33. If f (x) = $\begin{cases} xe^{-\left(\frac{1}{|x|} + \frac{1}{x}\right)}, & x \neq 0 \text{ then f (x) is} \\ 0, & x = 0 \end{cases}$
 - (A) continuous as well as differentiable for all x
 - (B) continuous for all x but not differentiable at x = 0
 - (C) neither differentiable nor continuous at x = 0
 - (D) discontinuous everywhere
- 34. If the function $f(x) = 2x^3 9ax^2 + 12a^2x + 1$, where a > 0, attains its maximum and minimum at p and q respectively such that $p^2 = q$, then a equals
 - (A) 3 (B) 1 (C) 2 (D) $\frac{1}{2}$

35. If
$$f(y) = e^y$$
, $g(y) = y$; $y > 0$ and $F(t) = \int_0^t f(t - y) g(y) dy$, then

(A) F (t) =
$$1 - e^{-t} (1 + t)$$

(C) F (t) = $t e^{t}$

(B) F (t) =
$$e^{t}$$
 – (1 + t)
(D) F (t) = $t e^{-t}$

(C) F (t) =
$$t e^{t}$$

(D) F (t) =
$$t e^{-t}$$

36. If
$$f(a + b - x) = f(x)$$
, then $\int_a^b x f(x) dx$ is equal to

(A)
$$\frac{a+b}{2}\int_{a}^{b}f(b-x)dx$$

(B)
$$\frac{a+b}{2}\int_{a}^{b} f(x)dx$$

(C)
$$\frac{b-a}{2}\int_{a}^{b}f(x)dx$$

(D)
$$\frac{a+b}{2}\int_{a}^{b}f(a+b-x)dx$$

37. The value of
$$\lim_{x\to 0} \frac{\int_{0}^{x^2} \sec^2 t \, dt}{x \sin x}$$
 is

38. The value of the integral
$$I = \int_{0}^{1} x (1 - x)^{n} dx$$
 is

(A)
$$\frac{1}{n+1}$$

(B)
$$\frac{1}{n+2}$$

(C)
$$\frac{1}{n+1} - \frac{1}{n+2}$$

(D)
$$\frac{1}{n+1} + \frac{1}{n+2}$$

$$39. \qquad \lim_{n \to \infty} \frac{1 + 2^4 + 3^4 + \dots + n^4}{n^5} - \lim_{n \to \infty} \frac{1 + 2^3 + 3^3 + \dots + n^3}{n^5} \ is$$

(A)
$$\frac{1}{30}$$

(B) zero

(C)
$$\frac{1}{4}$$

(D) $\frac{1}{5}$

40. Let
$$\frac{d}{dx} F(x) = \left(\frac{e^{\sin x}}{x}\right)$$
, $x > 0$. If $\int_{1}^{4} \frac{3}{x} e^{\sin x^3} dx = F(k) - F(1)$, then one of the possible values

of k, is

41. The area of the region bounded by the curves
$$y = |x - 1|$$
 and $y = 3 - |x|$ is

(A) 2 sq units

(B) 3 sq units

(C) 4 sq units

(D) 6 sq units

42. Let f (x) be a function satisfying f' (x) = f (x) with f (0) = 1 and g (x) be a function that satisfies
$$f(x) + g(x) = x^2$$
. Then the value of the integral $\int_{0}^{1} f(x) g(x) dx$, is

(A)
$$e - \frac{e^2}{2} - \frac{5}{2}$$

(B) e +
$$\frac{e^2}{2} - \frac{3}{2}$$

(C)
$$e - \frac{e^2}{2} - \frac{3}{2}$$

(D) e +
$$\frac{e^2}{2} + \frac{5}{2}$$

43. The degree and order of the differential equation of the family of all parabolas whose axis is x-axis, are respectively

(A) 2, 1

(B) 1, 2

(C) 3, 2

(D) 2, 3

The solution of the differential equation $(1 + y^2) + (x - e^{\tan^{-1} y}) \frac{dy}{dx} = 0$, is 44.

(A) $(x-2) = k e^{-tan^{-1}y}$

(B) $2xe^{2\tan^{-1}y} + k$

(C) $x e^{tan^{-1}y} = tan^{-1} y + k$

(D) $x e^{2 \tan^{-1} y} = e^{\tan^{-1} y} + k$

45. If the equation of the locus of a point equidistant from the points (a_1, b_1) and (a_2, b_2) is $(a_1$ a_2) x + $(b_1 - b_2)$ y + c = 0, then the value of 'c' is

(A) $\frac{1}{2}(a_2^2 + b_2^2 - a_1^2 - b_1^2)$

(B) $a_1^2 + a_2^2 + b_1^2 - b_2^2$

(C) $\frac{1}{2}(a_1^2 + a_2^2 - b_1^2 - b_2^2)$

(D) $\sqrt{a_1^2 + b_1^2 - a_2^2 - b_2^2}$

46. Locus of centroid of the triangle whose vertices are (a cos t, a sin t), (b sin t, - b cos t) and (1, 0), where t is a parameter, is

- (A) $(3x 1)^2 + (3y)^2 = a^2 b^2$ (C) $(3x + 1)^2 + (3y)^2 = a^2 + b^2$

- (B) $(3x 1)^2 + (3y)^2 = a^2 + b^2$ (D) $(3x + 1)^2 + (3y)^2 = a^2 b^2$

If the pair of straight lines $x^2 - 2pxy - y^2 = 0$ and $x^2 - 2qxy - y^2 = 0$ be such that each pair 47. bisects the angle between the other pair, then

(A) p = q

(B) p = -q

(C) pq = 1

(D) pq = -1

48. a square of side a lies above the x-axis and has one vertex at the origin. The side passing through the origin makes an angle α (0 < α < $\frac{\pi}{4}$) with the positive direction of x-axis. The equation of its diagonal not passing through the origin is

- (A) y ($\cos \alpha \sin \alpha$) x ($\sin \alpha \cos \alpha$) = a
- (B) y (cos α + sin α) + x (sin α cos α) = a
- (C) y ($\cos \alpha + \sin \alpha$) + x ($\sin \alpha + \cos \alpha$) = a
- (D) y (cos α + sin α) + x (cos α sin α) = a

If the two circles $(x-1)^2 + (y-3)^2 = r^2$ and $x^2 + y^2 - 8x + 2y + 8 = 0$ intersect in two distinct 49. points, then

(A) 2 < r < 8

(B) r < 2

(C) r = 2

(D) r > 2

50. The lines 2x - 3y = 5 and 3x - 4y = 7 are diameters of a circle having area as 154 sq units. Then the equation of the circle is

(B) $x^2 + y^2 + 2x - 2y = 47$ (D) $x^2 + y^2 - 2x + 2y = 62$

(A) $x^2 + y^2 + 2x - 2y = 62$ (C) $x^2 + y^2 - 2x + 2y = 47$

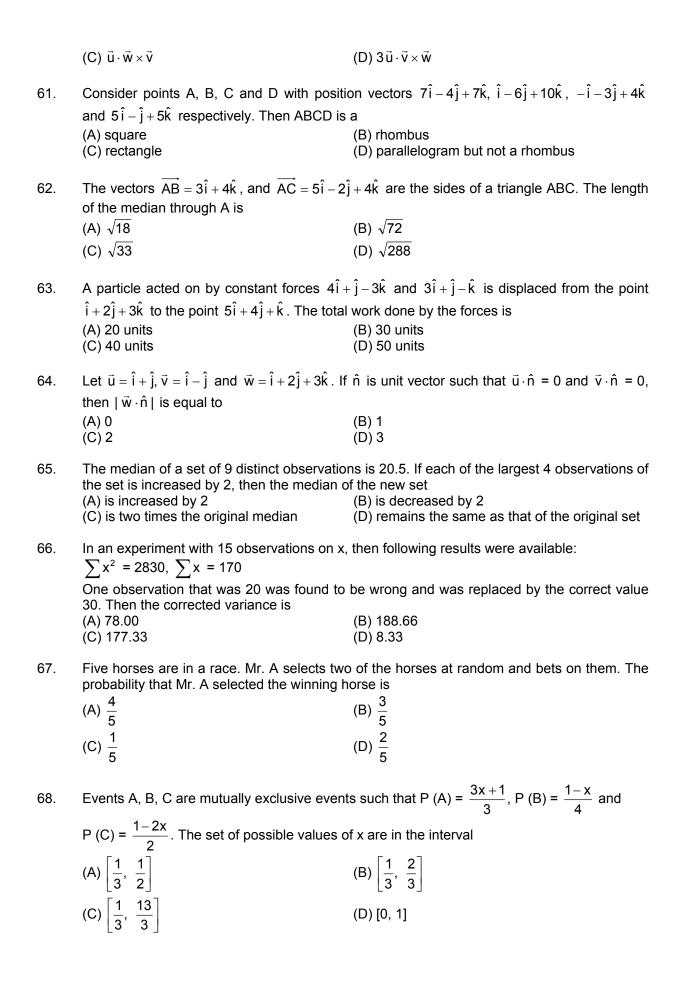
The normal at the point (bt₁², 2bt₁) on a parabola meets the parabola again in the point (bt₂², 51. 2bt₂), then

| (A) $t_2 = -t_1 - \frac{2}{t_1}$ | (B) $t_2 = -t_1 + \frac{2}{t_1}$ |
|----------------------------------|----------------------------------|
| (D) $t_2 = t_1 - \frac{2}{t_1}$ | (D) $t_2 = t_1 + \frac{2}{t_1}$ |
| | |

- 52. The foci of the ellipse $\frac{x^2}{16} + \frac{y^2}{b^2} = 1$ and the hyperbola $\frac{x^2}{144} \frac{y^2}{81} = \frac{1}{25}$ coincide. Then the value of b^2 is
 - value of b² is
 (A) 1 (B) 5
 (C) 7 (D) 9
- 53. A tetrahedron has vertices at O (0, 0, 0), A (1, 2, 1), B (2, 1, 3) and C (– 1, 1, 2). Then the angle between the faces OAB and ABC will be
 - (A) $\cos^{-1}\left(\frac{19}{35}\right)$ (B) $\cos^{-1}\left(\frac{17}{31}\right)$ (C) 30° (D) 90°
- 54. The radius of the circle in which the sphere $x^2 + y^2 + z^2 + 2x 2y 4z 19 = 0$ is cut by the plane x + 2y + 2z + 7 = 0 is

 (B) 2
 - (A) 1 (B) 2 (C) 3 (D) 4
- 55. The lines $\frac{x-2}{1} = \frac{y-3}{1} = \frac{z-4}{-k}$ and $\frac{x-1}{k} = \frac{y-4}{2} = \frac{z-5}{1}$ are coplanar if

 (A) k = 0 or -1(B) k = 1 or -1(C) k = 0 or -3
- 56. The two lines x = ay + b, z = cy + d and x = a'y + b', z = c'y + d' will be perpendicular, if and only if
 - (A) aa' + bb' + cc' + 1 = 0 (B) aa' + bb' + cc' = 0 (C) (a + a')(b + b') + (c + c') = 0 (D) aa' + cc' + 1 = 0
- 57. The shortest distance from the plane 12x + 4y + 3z = 327 to the sphere $x^2 + y^2 + z^2 + 4x 2y 6z = 155$ is
 - (A) 26 (B) $11\frac{4}{13}$ (C) 13 (D) 39
- 58. Two systems of rectangular axes have the same origin. If a plane cuts them at distances a, b, c and a', b', c' from the origin, then
 - (A) $\frac{1}{a^2} + \frac{1}{b^2} + \frac{1}{c^2} + \frac{1}{a'^2} + \frac{1}{b'^2} + \frac{1}{c'^2} = 0$ (B) $\frac{1}{a^2} + \frac{1}{b^2} \frac{1}{c^2} + \frac{1}{a'^2} + \frac{1}{b'^2} \frac{1}{c'^2} = 0$ (C) $\frac{1}{a^2} \frac{1}{b^2} \frac{1}{c^2} + \frac{1}{a'^2} \frac{1}{b'^2} \frac{1}{c'^2} = 0$ (D) $\frac{1}{a^2} + \frac{1}{b^2} + \frac{1}{c^2} \frac{1}{a'^2} \frac{1}{b'^2} \frac{1}{c'^2} = 0$
- 59. \vec{a} , \vec{b} , \vec{c} are 3 vectors, such that $\vec{a} + \vec{b} + \vec{c} = \vec{0}$, $|\vec{a}| = 1$, $|\vec{b}| = 2$, $|\vec{c}| = 3$, then $\vec{a} \cdot \vec{b} + \vec{b} \cdot \vec{c} + \vec{c} \cdot \vec{a}$ is equal to
 - (A) 0 (C) 7 (B) – 7 (D) 1
- 60. If \vec{u} , \vec{v} and \vec{w} are three non-coplanar vectors, then $(\vec{u} + \vec{v} \vec{w}) \cdot (\vec{u} \vec{v}) \times (\vec{v} \vec{w})$ equals (A) 0 (B) $\vec{u} \cdot \vec{v} \times \vec{w}$



| 69. | The mean and variance of a random variable having a binomial distribution are 4 and respectively, then $P(X = 1)$ is | | |
|-----|---|---|--|
| | (A) $\frac{1}{32}$ | (B) $\frac{1}{16}$ (D) $\frac{1}{4}$ | |
| | (C) $\frac{1}{8}$ | (D) $\frac{1}{}$ | |
| | ` ' 8 | ` ' 4 | |
| 70. | The resultant of forces \vec{P} and \vec{Q} is \vec{R} . If \vec{Q} is reversed, then \vec{R} is again doubled. The (A) $3:1:1$ (C) $1:2:3$ | is doubled then \vec{R} is doubled. If the direction of then $P^2:Q^2:R^2$ is (B) $2:3:2$ (D) $2:3:1$ | |
| 71. | Let R ₁ and R ₂ respectively be the maximum the maximum range on the horizontal plane (A) arithmetic–geometric progression (C) G.P. | ranges up and down an inclined plane and R be . Then R_1 , R , R_2 are in (B) A.P. (D) H.P. | |
| 72. | A couple is of moment \vec{G} and the force forming the couple is \vec{P} . If \vec{P} is turned through a right angle, the moment of the couple thus formed is \vec{H} . If instead, the forces \vec{P} are turned through an angle α , then the moment of couple becomes | | |
| | (A) $\vec{G} \sin \alpha - \vec{H} \cos \alpha$ | (B) $\vec{H} \cos \alpha + \vec{G} \sin \alpha$ | |
| | (C) $\vec{G} \cos \alpha - \vec{H} \sin \alpha$ | (D) $\vec{H} \sin \alpha - \vec{G} \cos \alpha$ | |
| 73. | Two particles start simultaneously from the same point and move along two straight line one with uniform velocity \vec{u} and the other from rest with uniform acceleration \vec{f} . Let α be the angle between their directions of motion. The relative velocity of the second particle where respect to the first is least after a time | | |
| | (A) $\frac{u \sin \alpha}{f}$ | (B) $\frac{f\cos\alpha}{u}$ | |
| | (C) $u \sin \alpha$ | (D) $\frac{u\cos\alpha}{f}$ | |
| 74. | Two stones are projected from the top of a cliff h meters high, with the same speed u so as to hit the ground at the same spot. If one of the stones is projected horizontally and the other is projected at an angle θ to the horizontal then tan θ equals | | |
| | (A) $\sqrt{\frac{2u}{gh}}$ | (B) $2g\sqrt{\frac{u}{h}}$ | |
| | (C) $2h\sqrt{\frac{u}{g}}$ | (D) $u\sqrt{\frac{2}{gh}}$ | |
| 75. | A body travels a distances s in t seconds. It starts from rest and ends at rest. In the first p of the journey, it moves with constant acceleration f and in the second part with const retardation r. The value of t is given by | | |
| | (A) $2s\left(\frac{1}{f} + \frac{1}{r}\right)$ | (B) $\frac{2s}{\frac{1}{f} + \frac{1}{r}}$ | |
| | (C) $\sqrt{2s(f+r)}$ | (D) $\sqrt{2s\left(\frac{1}{f} + \frac{1}{r}\right)}$ | |

Solutions

1. Clearly both one – one and onto

Because if n is odd, values are set of all non-negative integers and if n is an even, values are set of all negative integers.

Hence, (C) is the correct answer.

2. $z_1^2 + z_2^2 - z_1 z_2 = 0$ $(z_1 + z_2)^2 - 3z_1 z_2 = 0$ $a^2 = 3b$.

Hence, (C) is the correct answer.

5. $\begin{vmatrix} a & a^{2} & 1 \\ b & b^{2} & 1 \\ c & c^{2} & 1 \end{vmatrix} + \begin{vmatrix} 1 & a & a^{2} \\ 1 & b & b^{2} \\ 1 & c & c^{2} \end{vmatrix} = 0$ $(1 + abc) \begin{vmatrix} a & a^{2} & 1 \\ b & b^{2} & 1 \\ c & c^{2} & 1 \end{vmatrix} = 0$

$$\Rightarrow$$
 abc = -1 .

Hence, (B) is the correct answer

4. $\frac{1+i}{1-i} = \frac{(1+i)^2}{2} = i$

$$\left(\frac{1+i}{1-i}\right)^{x} = i^{x}$$

$$\Rightarrow$$
 x = 4n.

Hence, (A) is the correct answer.

6. Coefficient determinant = $\begin{vmatrix} 1 & 2a & a \\ 1 & 3b & b \\ 1 & 4c & c \end{vmatrix} = 0$

$$\Rightarrow$$
 b = $\frac{2ac}{a+c}$.

Hence, (C) is the correct answer

8. $x^2 - 3|x| + 2 = 0$

$$(|x|-1)(|x|-2)=0$$

$$\Rightarrow$$
 x = \pm 1, \pm 2.

Hence, (B) is the correct answer

7. Let α , β be the roots

$$\alpha + \beta = \frac{1}{\alpha^2} + \frac{1}{\beta^2}$$

$$\alpha + \beta = \frac{\alpha^2 + \beta^2 - 2\alpha\beta}{(\alpha + \beta)}$$

$$\left(-\frac{b}{a}\right) = \frac{b^2 - 2ac}{c^2}$$

$$\Rightarrow$$
 2a²c = b (a² + bc)

$$\Rightarrow \frac{a}{c}, \frac{b}{a}, \frac{c}{b}$$
 are in H.P.

Hence, (C) is the correct answer

10.
$$A = \begin{bmatrix} a & b \\ b & a \end{bmatrix}$$
$$A^{2} = \begin{bmatrix} a & b \\ b & a \end{bmatrix} \begin{bmatrix} a & b \\ b & a \end{bmatrix}$$
$$= \begin{bmatrix} a^{2} + b^{2} & 2ab \\ 2ab & a^{2} + b^{2} \end{bmatrix}$$
$$\Rightarrow \alpha = a^{2} + b^{2}, \beta = 2ab.$$

Hence, (B) is the correct answer.

9.
$$\beta = 2\alpha$$

$$3\alpha = \frac{3a-1}{a^2-5a+3}$$

$$2\alpha^2 = \frac{2}{a^2-5a+6}$$

$$\frac{(3a-1)^2}{a(a^2-5a+3)^2} = \frac{1}{a^2+5a+6}$$

$$\Rightarrow a = \frac{2}{3}.$$

Hence, (A) is the correct answer

- 12. Clearly $5! \times 6!$ (A) is the correct answer
- 11. Number of choices = ${}^5C_4 \times {}^8C_6 + {}^5C_5 \times {}^8C_5$ = 140 + 56. Hence, (B) is the correct answer

13.
$$\Delta = \begin{vmatrix} 1 + \omega^{n} + \omega^{2n} & \omega^{n} & \omega^{2n} \\ 1 + \omega^{n} + \omega^{2n} & \omega^{2n} & 1 \\ 1 + \omega^{n} + \omega^{2n} & 1 & \omega^{n} \end{vmatrix}$$

Since, $1 + \omega^n + \omega^{2n} = 0$, if n is not a multiple of 3 Therefore, the roots are identical. Hence, (A) is the correct answer

14.
$${}^{n}C_{r+1} + {}^{n}C_{r-1} + {}^{n}C_{r} + {}^{n}C_{r}$$

$$= {}^{n+1}C_{r+1} + {}^{n+1}C_{r}$$

$$= {}^{n+2}C_{r+1} + {}^{n+1}C_{r}$$

Hence, (B) is the correct answer

17.
$$\frac{1}{1 \cdot 2} - \frac{1}{2 \cdot 3} + \frac{1}{3 \cdot 4} - \dots$$
$$= 1 - \frac{1}{2} - \frac{1}{2} + \frac{1}{3} + \frac{1}{3} - \frac{1}{4} - \dots$$

$$= 1 - 2\left(\frac{1}{2} - \frac{1}{3} + \frac{1}{4} - \dots\right)$$

$$= 2\left(1 - \frac{1}{2} + \frac{1}{3} - \frac{1}{4} + \dots\right) - 1$$

$$= 2 \log 2 - \log e$$

$$= \log\left(\frac{4}{e}\right).$$

Hence, (D) is the correct answer.

- 15. General term = 256 C_r ($\sqrt{3}$) $^{256-r}$ [(5) $^{1/8}$]^r From integral terms, or should be 8k \Rightarrow k = 0 to 32. Hence, (B) is the correct answer.
- 18. $f(x) = ax^2 + bx + c$ f(1) = a + b + c f(-1) = a - b + c $\Rightarrow a + b + c = a - b + c$ also 2b = a + c f'(x) = 2ax + b = 2ax $f'(a) = 2a^2$ f'(b) = 2ab f'(c) = 2ac $\Rightarrow AP$. Hence, (A) is the correct answer.
- 19. Result (A) is correct answer.
- 20. (B)

21.
$$a\left(\frac{1+\cos C}{2}\right) + c\left(\frac{1+\cos A}{2}\right) = \frac{3b}{2}$$

$$\Rightarrow a+c+b=3b$$

$$a+c=2b.$$
Hence, (A) is the correct answer

26.
$$f(1) = 7$$

$$f(1 + 1) = f(1) + f(1)$$

$$f(2) = 2 \times 7$$
only $f(3) = 3 \times 7$

$$\sum_{r=1}^{n} f(r) = 7 (1 + 2 + \dots + n)$$

$$= 7 \frac{n(n+1)}{2}.$$

25. (B)

23.
$$-\frac{\pi}{4} \le \frac{\sin^2 x}{2} \le \frac{\pi}{4}$$
 $-\frac{\pi}{4} \le \sin^{-1}(a) \le \frac{\pi}{4}$

$$\frac{1}{2} \le |a| \le \frac{1}{\sqrt{2}}.$$

Hence, (D) is the correct answer

27. LHS =
$$1 - \frac{n}{1!} + \frac{n(n-1)}{2!} - \frac{n(n-1)(n-2)}{3!} + \dots$$

= $1 - {^{n}C_{1}} + {^{n}C_{2}} - \dots$

Hence, (C) is the correct answer

30.
$$\lim_{x\to 0} \frac{\frac{1}{3+x} + \frac{1}{3-x}}{1} = \frac{2}{3}.$$

Hence, (C) is the correct answer.

28.
$$4 - x^{2} \neq 0$$

$$\Rightarrow x \neq \pm 2$$

$$x^{3} - x > 0$$

$$\Rightarrow x (x + 1) (x - 1) > 0.$$
Hence (D) is the correct answer.

29.
$$\lim_{x \to \pi/2} \frac{\tan\left(\frac{\pi}{4} - \frac{x}{2}\right)(1 - \sin x)}{4\left(\frac{\pi}{4} - \frac{x}{2}\right)(\pi - 2x)^2}$$
$$= \frac{1}{32}.$$

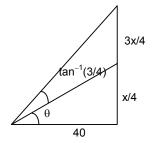
Hence, (C) is the correct answer.

32.
$$f(-x) = -f(x)$$

Hence, (B) is the correct answer.

1.
$$\sin (\theta + \alpha) = \frac{x}{40}$$

 $\sin a = \frac{x}{140}$
 $\Rightarrow x = 40$.
Hence, (B) is the correct answer



34.
$$f(x) = 0$$
 at $x = p$, q
 $6p^2 + 18ap + 12a^2 = 0$
 $6q^2 + 18aq + 12a^2 = 0$
 $f''(x) < 0$ at $x = p$
and $f''(x) > 0$ at $x = q$.

30. Applying L. Hospital's Rule
$$\lim_{x\to 2a} \frac{f(a)g'(a) - g(a)f'(a)}{g'(a) - f'(a)} = 4$$

$$\frac{\mathsf{k}(\mathsf{g}'(\mathsf{a})-\mathsf{f}'(\mathsf{a}))}{(\mathsf{g}'(\mathsf{a})-\mathsf{f}'(\mathsf{a}))}=4$$

k = 4

Hence, (A) is the correct answer.

36.
$$\int_{a}^{b} x f(x) dx$$

$$= \int_{a}^{b} (a+b-x) f(a+b-x) dx.$$

Hence, (B) is the correct answer.

33.
$$f'(0)$$

$$f'(0-h) = 1$$

$$f'(0+h) = 0$$

$$LHD \neq RHD.$$
Hence, (B) is the correct answer.

37.
$$\lim_{x \to 0} \frac{\tan(x^2)}{x \sin x}$$
$$= \lim_{x \to 0} \frac{\tan(x^2)}{x^2 \left(\frac{\sin x}{x}\right)}$$

Hence (C) is the correct answer.

38.
$$\int_{0}^{1} x (1-x)^{n} dx = \int_{0}^{1} x^{n} (1-x)$$
$$= \int_{0}^{1} (x^{n} - x^{n+1}) = \frac{1}{n+1} - \frac{1}{n+2}.$$

Hence, (C) is the correct answer.

35.
$$F(t) = \int_{0}^{t} f(t - y) f(y) dy$$
$$= \int_{0}^{t} f(y) f(t - y) dy$$
$$= \int_{0}^{t} e^{y} (t - y) dy$$
$$= x^{t} - (1 + t).$$

Hence, (B) is the correct answer.

34. Clearly
$$f''(x) > 0$$
 for $x = 2a \Rightarrow q = 2a < 0$ for $x = a \Rightarrow p = a$ or $p^2 = q \Rightarrow a = 2$. Hence, (C) is the correct answer.

40.
$$F'(x) = \frac{e^{\sin x}}{3^x}$$

$$= \int \frac{3}{x} e^{\sin x} dx = F(k) - F(1)$$

$$= \int_{1}^{64} \frac{e^{\sin x}}{x} dx = F(k) - F(1)$$

$$= \int_{1}^{64} F'(x) dx = F(k) - F(1)$$

$$= \int_{1}^{64} F'(x) dx = F(k) - F(1)$$

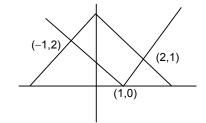
$$\Rightarrow k = 64.$$

$$F(64) - F(1) = F(k) - F(1)$$

Hence, (D) is the correct answer.

41. Clearly area =
$$2\sqrt{2} \times \sqrt{2}$$

= sq units



45. Let p (x, y)

$$(x - a_1)^2 + (y - b_1)^2 = (x - a_2)^2 + (y - b_2)^2$$

$$(a_1 - a_2) x + (b_1 - b_2) y + \frac{1}{2} (b_2^2 - b_1^2 + a_2^2 - a_1^2) = 0.$$

Hence, (A) is the correct answer.

46.
$$x = \frac{a\cos t + b\sin t + 1}{3}, y = \frac{a\sin t - b\cos t + 1}{3}$$

$$\left(x - \frac{1}{3}\right)^2 + y^2 = \frac{a^2 + b^2}{9}.$$

Hence, (B) is the correct answer.

43. Equation
$$y^2 = 4a 9x - h$$
)
 $2yy_1 = 4a \Rightarrow yy_1 = 2a$
 $yy_2 = y_1^2 = 0$.
Hence (B) is the correct answer.

42.
$$\int_{0}^{1} f(x)[x^{2} - f(x)] dx$$
solving this by putting f'(x) = f(x).
Hence, (B) is the correct answer.

50. Intersection of diameter is the point
$$(1, -1)$$

$$\pi s^2 = 154$$

$$\Rightarrow s^2 = 49$$

$$(x - 1)^2 + (y + 1)^2 = 49$$
Hence, (C) is the correct answer.
47. (D)

49.
$$\frac{dx}{dy} (1 + y^2) = (e^{\sin^{-1} y} - x)$$

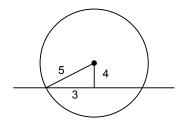
(D)

$$\frac{dx}{dy} + \frac{x}{1+y^{\alpha}} = \frac{e^{sub^{-1}-y}}{1+y^2}$$

52.
$$\frac{x^2}{\left(\frac{12}{5}\right)^2} - \frac{y^2}{\left(\frac{9}{5}\right)^2} = 1$$
$$\Rightarrow e_1 = \frac{5}{4}$$
$$ae_2 = \sqrt{1 - \frac{b^2}{16}} \times 4 = 3$$
$$\Rightarrow b^2 = 7.$$

Hence, (C) is the correct answer.

54. (C)



Hence, (A) is the correct answer.

49.
$$(x-1)^2 + (y-3)^2 = r^2$$

 $(x-4)^2 + (y+2)^2 - 16 - 4 + 8 = 0$
 $(x-4)^2 + (y+2)^2 = 12$.

67. Select 2 out of 5
$$= \frac{2}{5}.$$
Hence (D) is the core

Hence, (D) is the correct answer.

65.
$$0 \le \frac{3x+1}{3} + \frac{1-x}{4} + \frac{1-2x}{2} \le 1$$

$$12x+4+3-3x+6-12x \le 1$$

$$0 \le 13-3x \le 12$$

$$3x \le 13$$

$$\Rightarrow x \ge \frac{1}{3}$$

$$x \le \frac{13}{3}.$$

Hence, (C) is the correct answer.

3.
$$\operatorname{Arg}\left(\frac{z}{\omega}\right) = \frac{\pi}{2}$$
$$|z\omega| = 1$$
$$\overline{z}\omega = -i \text{ or } +i.$$

$$|z\omega| = 1$$

$$\overline{z}\omega = -i \text{ or } + i$$
.